Optically optimal wavelength-scale patterned ITO/ZnO composite coatings for thin film solar cells

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(Received 3 January 2012; accepted 9 March 2012; published online 17 April 2012)

A methodology is proposed for finding structures that are, optically speaking, locally optimal: a physical analysis of much simpler structures is used to constrain the optimization process. The obtained designs are based on a flat amorphous silicon layer (to minimize recombination) with a patterned anti-reflective coating made of ITO or ZnO, or a composite ITO/ZnO coating. These latter structures are realistic and present good performances despite very thin active layers. © 2012 American Institute of Physics. [http://dx.doi.org/10.1063/1.3703670]

I. INTRODUCTION

Thanks to the maturity of nanophotonics, various advanced light trapping schemes suited to photovoltaic solar cells have been proposed and investigated in recent years. The interest of these novel approaches is to generate highly efficient anti-reflecting structures,1–7 but also, and maybe more importantly, to increase significantly the absorption efficiency in the long wavelength range, where active media are generally less efficient, and finally to reduce the thickness of the absorbing layers. Different groups have been focusing on the possibility to pattern the absorbing layers like crystalline or amorphous silicon.8–11 This leads to a high absorption enhancement, but the positive impact on the conversion efficiency is still to be assessed. Indeed, the increased area corresponding to the free and processed surfaces may lead to extensive surface recombination. Moreover, the designs generally result from simple design rules, or geometrical parameter scanning. There is therefore a strong need to develop more advanced methodologies, in order to optimize the design of these advanced solar cells. In this paper, our goals are to (1) propose a design methodology based on a purely numerical optimization, guided by a physical analysis, that would be able to make locally optimal structures emerge from the process and (2) provide designs for solar cell structures including an anti-reflective layer patterned as a photonic lattice and compatible with a low level of surface recombinations, using the previous methodology.

Here we will consider both flat and periodically patterned anti-reflective coatings made of ITO and ZnO, the two most common materials used as transparent conducting electrodes. We carry on a thorough study of the simplest structures and use genetic algorithms guided by our physical analysis to optimize grating structures. This will lead us to propose hybrid anti-reflective coatings made of ITO and ZnO, to combine the optical properties of ZnO (which exhibits a high refractive index and a low absorption coefficient)12 with the electrical properties of ITO (which is more conductive, but also more absorbent). The structures we propose are finally very thin (typically thinner than 300 nm), but present surprisingly good efficiencies. These structures can thus be considered as an extremely efficient way to use silicon to convert light into electron–hole pairs and may be relatively inexpensive to produce.

II. FLAT ANTI-REFLECTIVE COATINGS

The goal of this section is to look for very simple, but optically optimal structures and to understand the physical reasons why these structures are locally optimal. This will allow us to guide the numerical optimization of the more complex structures that will be studied in Sec. III.

In this section, we will consider flat anti-reflective coatings made of ZnO or ITO [as shown in Fig. 1(a)], or bi-layer hybrid coatings with an ITO layer for electrical reasons and a ZnO layer on top to improve the optical properties of the coating [see Fig. 1(b)]. A thickness of 30 nm has been considered for the ITO layer in the case of a hybrid coating. Reducing the ITO thickness down to 30 nm, compared to a more standard value around 50–70 nm,13 yields a lower useless absorption in the transparent conduction oxide layer. This reduction is made possible in the case of our hybrid design, since the top ZnO layer will also contribute to the lateral conduction of electrical charges.

The amorphous silicon ($a$-Si:H) layer stands above a perfect electric conductor for simplicity, and to be able to compare with previous works on this subject,6 some of them being particularly reliable and thorough.3

The figure of merit in all our work is the short-circuit current under normal illumination. We assume that all the photons absorbed by the silicon are converted into electron–hole pairs and that all the carriers produced contribute to the current—the recombinations of the electron–hole pairs being minimized when considering a thin enough, flat $a$-Si:H layer. The short-circuit current can in that case be written as

with the electrical properties of ITO (which is more conductive, but also more absorbent). The structures we propose are finally very thin (typically thinner than 300 nm), but present surprisingly good efficiencies. These structures can thus be considered as an extremely efficient way to use silicon to convert light into electron–hole pairs and may be relatively inexpensive to produce.
\[ j_{sc} = \int A(\lambda) \frac{dI}{d\lambda} \frac{e^\lambda}{hc} d\lambda, \quad (1) \]

where \( \lambda \) is the wavelength, ranging from 375 nm (beginning of the solar spectrum) to 750 nm (above which the a-Si:H becomes transparent), \( dI/d\lambda \) is the spectral energy density of the light source (we have taken an am1.5 normalized spectrum), and \( A(\lambda) \) is the absorption of the a-Si:H layer (see the Appendix for details regarding the numerical computation of the absorption). If all the incoming photons of the considered spectral range were converted into electron–hole pairs, the short-circuit current would be equal to \( j_0 = 23.665 \) mA/cm\(^2\). The conversion efficiency (CE) is given by the fraction of the incoming photons that are converted into electron–hole pairs, i.e., \( CE = j_{sc}/j_0 \).

Figure 2 shows the conversion efficiency of the structure when either ZnO or ITO anti-reflective coatings (on top of a 100 nm thick a-Si:H layer) are considered, as a function of the coating thickness \( h_1 \). It appears clearly that there is an obvious optimal thickness around 52 nm for ZnO (and 56 nm for ITO) for a 100 nm thick silicon layer. This optimal thickness for the coating is accurate: the efficiency is roughly 20% smaller for a 100 nm anti-reflective coating in both cases. This behavior is universal and does not depend on the thickness of the amorphous silicon layer, even if the optimal thickness slightly depends on the a-Si:H thickness.

For thick ZnO layers, the absorption tends to a limit that is 10% below the maximum (this difference is even worse for thicker silicon layers). For ITO, the absorption by the silicon layer is a decreasing function of the thickness due to the absorption by the coating itself. This confirms that thin and higher index anti-reflective coatings are a better solution from an optical point of view, as long as the losses can be neglected. However, ZnO does not present a very high conductivity, so that it is usually necessary to use very thick ZnO layers. That is obviously detrimental to the optical properties, hence the idea to combine a thin ITO layer with a ZnO layer. The resulting anti-reflective coating presents intermediary optical properties, as shown in Fig. 2, making this structure a very interesting trade-off.

Let us now study how the absorption could be influenced by the thickness of the a-Si:H layer itself, when an optimal anti-reflective coating is assumed (i.e., for each thickness of the a-Si:H layer, the optimal thickness of the anti-reflective coating is computed and used to find the CE). The results are shown in Fig. 3. The absorption is not a strictly increasing function of the silicon layer thickness, as long as this thickness is smaller than 300 nm. This means that there are clear local maxima of the CE, and that this thickness should probably not be chosen arbitrarily when it is small.

Figure 3 shows three local maxima, whatever the anti-reflective coating. The first two maxima are more pronounced than the third one, and since they happen for small values of the thickness, these maxima correspond to structures making a much more efficient use of silicon; that is especially true for the first maximum, but the second one definitely presents a higher efficiency that could be interesting, too. The characteristics of these structures are detailed Table I.

Physically, the efficiency of an anti-reflective coating relies on the resonances it may support: any resonance is
associated with a high transmission of light to the underlying medium. If the anti-reflective coating presents an index that is intermediate between the active layer and the superstrate (the superstrate being air, this is the case for ITO and ZnO here), these resonances occur when \( \lambda \simeq 4hn/(1 + 2m) \), where \( h \) is the thickness and \( n \) the index of the dielectric layer and \( m \) is the order of the resonance. Figure 4 shows absorption spectra for the optimal thickness of a ZnO layer and for a much thicker layer. For thick layers, the resonances are numerous and narrow. Slightly changing the thickness in this regime will just shift the resonances a little, but since the resonances and the anti-resonances will be averaged over the whole spectrum, the change in the thickness has little impact on the overall efficiency. On the contrary, a very thin anti-reflective coating supports essentially one resonance around \( \lambda \simeq 4hn(\lambda) \). This position of this broad resonance has a great impact on the CE and it can be tuned to maximize the efficiency: the optimal position for the resonance seems to be located where the silicon is the most absorbent. According to the above-presented formula, a thickness of 51 nm should produce a resonance around 435 nm, which is totally consistent with the spectra shown in Fig. 4. That is why the efficiency is very sensitive to the thickness of the coating for thin layers, and why thin coatings are more efficient.6

Let us now consider the impact of the silicon layer on the CE. The \( a\)-Si:H layer can support cavity resonances when the penetration length is smaller than the thickness. A typical absorption spectrum for a thick layer without any anti-reflective coating is shown in Fig. 4. For short wavelength (\( \lambda < 550 \) nm), the amorphous silicon is very absorbent and the spectrum is almost flat. Several resonances can be seen on the spectrum for longer wavelength. As already discussed for the anti-reflective coating, these resonances are narrow because of the layer’s thickness. Any change in the thickness is likely to increase the conversion efficiency, but only slightly. On the contrary, thin \( a\)Si:H layers (compared to the penetration length) may support broad resonances over almost the whole spectrum. As shown in Fig. 4, an 87 nm thick silicon layer without any coating supports essentially one broad resonance in the middle of the visible spectrum. This resonance still appears as a shoulder on the spectrum of the structure with the optimal anti-reflective coating. Finally, these carefully optimized cells present good theoretical efficiencies.

Let us consider a typical non-optimized flat structure, also considered in Ref. 3. The structure is a 300 nm thick \( a\)-Si:H layer, backed by a 19 nm ZnO layer and a perfect electric conductor, with a 1024 nm thick ZnO coating. According to our simulations, it presents an efficiency of 53.3% on the range of the spectrum considered here (our simulations are generally in an excellent agreement with all the results presented in Kroll et al. (Ref. 3)). This structure is typical essentially because, for electrical reasons, it presents a very thick transparent oxide layer.

By comparison, the locally optimal structures we propose are able to reach a similar efficiency with much less silicon (three times less silicon typically in this case). This is, of course, partly due to the optimized anti-reflective coating, and can be seen as an illustration that, as shown in Fig. 3, it is relatively easy to reach interesting efficiencies with thin active layers, while any further increase of the efficiency may generally require a large supplementary amount of silicon.

### III. PATTERNED COATINGS

It is well known that structuring the silicon or the electrode layer can have a great impact on absorption, leading to increased efficiencies. In this section, the impact of the patterning of the anti-reflective coating only on the conversion efficiency is assessed. Our goal is still to find optically (and at least locally) optimal structures with a flat and as thin as possible amorphous silicon layer, to minimize recombination. The structures we consider are shown in Fig. 5.

The optical behavior of these structures is complex, and their geometry is controlled by many parameters. The optimization cannot be done manually as has been done earlier in this paper. Homemade genetic algorithms15 were thus used to find parameters corresponding to a maximum conversion efficiency.

Had we just ran an unconstrained optimization, the result would have been a very thick active layer. But the previous physical analysis of the flat structures gives a strong indication that locally optimal structures may exist even for more complex structures. In order to find these local optima,
the genetic algorithm has been constrained. Since we expected the optimal patterned structures to resemble somehow the flat ones, we have used different constraints based on the above-presented results. The algorithm was allowed to consider only structures with $h_{Si} < 150$ nm, or with $h_{Si} < 200$ nm (or even with $h_{Si} < 250$ nm).

The algorithm was able to find optimal structures, thus establishing the existence of local optima. The results are summarized in Table II. They show that the patterned optimal structures are very close to the flat ones: the thickness of the active layer is very close in both cases, as is the thickness of the homogeneous part of the anti-reflective coating. This is what allows us to conclude that the physical behavior of the structures is still dominated by the phenomena studied in the previous section: the resonances inside the silicon layer and the homogeneous (unpatterned) part of the anti-reflective coating.

Moreover, let us just underline the following:

(1) The patterning is obviously not interesting for the ITO coating: any increase of the ITO thickness is detrimental to the optical properties and the advantages of the patterning are not large enough to overcome that drawback—so that the flat structure seems to be very close to the optimal solution in that case.

(2) The ZnO coating presents once more the best optical properties. It is possible to compare similar patterned and non-patterned structures. The patterning brings an increase of 13% in the conversion efficiency for the thinnest structure and of 7% for the second optimum.

(3) The performances of the composite coatings are close to the performances of ZnO coatings here too. The patternning brings a 10% (respectively, 6.2%) increase of the conversion efficiency for the first optimum (respectively, the second optimum).

Physically, two mechanisms can explain the efficiency of the grating: (1) it is a supplementary layer with a different effective index, making the anti-reflective coating more effective for different wavelength; (2) it allows one to excite guided modes inside the active layer, leading to an enhanced absorption at longer wavelength where the amorphous silicon can be considered almost completely transparent.

Figure 6 shows the absorption spectrum for the optimal structures with a ZnO coating. The red curves on Fig. 4 (optimal flat ZnO layer) and Fig. 6 (optimal patterned ZnO coating) can be compared. The anti-reflective behavior persists in the same way in the blue part of the spectrum. The most obvious difference is the peak that can be seen around 600 nm. This can perfectly be understood if the whole ZnO structure is seen as a double layer optical filter. The numerical method we use (see the Appendix and Ref. 16) gives access to the modes propagating inside a ZnO grating layer (corresponding to the first ZnO structure in Table II). Two modes are actually propagative: the first one has an effective index of 1.687 at 600 nm, and the second one presents a lower index of 0.1149. The first mode can be considered responsible for the transmission of this layer, the other being only slightly excited by the incident plane wave. Adding the grating layer can thus be seen as adding another homogeneous layer with a well defined refractive index to an optical filter, and a simple simulation17 shows that the resulting anti-reflective coating presents a transmission peak at 600 nm in

![FIG. 5. Structured anti-reflective coating. The geometrical parameters are $h_{Si}$, the thickness of the silicon layer, $d$ the period of the grating, $h_r$ its height, and $f$ the fill factor, while $h_{i1}$ is the thickness of the layer between the silicon and the grating.](image)

![FIG. 6. Absorption of the first optimum for a ZnO coating (black line), of a 94 nm a-Si:H slab (the black dashed line corresponds to the bare silicon layer), and of the first optimal grating structure (ZnO, $h_{Si} < 150$ nm; red line: TE polarization, blue line: TM polarization).](image)

<table>
<thead>
<tr>
<th>Structure</th>
<th>$h_{Si}$ (nm)</th>
<th>$h_{i1}$ (nm)</th>
<th>$f$</th>
<th>$d$ (nm)</th>
<th>$h_r$ (nm)</th>
<th>CE</th>
<th>$j_{sc}$ (mA/cm²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ITO, $h_{Si} &lt; 150$ nm</td>
<td>91.6</td>
<td>39.35</td>
<td>0.355</td>
<td>434.4</td>
<td>44.0</td>
<td>50.96</td>
<td>12.06</td>
</tr>
<tr>
<td>ZnO, $h_{Si} &lt; 150$ nm</td>
<td>94</td>
<td>207</td>
<td>0.35</td>
<td>439</td>
<td>53.5</td>
<td>61.3</td>
<td>14.5</td>
</tr>
<tr>
<td>Hybrid, $h_{Si} &lt; 150$ nm</td>
<td>96.5</td>
<td>205</td>
<td>0.37</td>
<td>445</td>
<td>24.1</td>
<td>58.15</td>
<td>13.8</td>
</tr>
<tr>
<td>ITO, $h_{Si} &lt; 200$ nm</td>
<td>174.3</td>
<td>25.1</td>
<td>0.633</td>
<td>385.9</td>
<td>43.2</td>
<td>56.2</td>
<td>13.3</td>
</tr>
<tr>
<td>ZnO, $h_{Si} &lt; 200$ nm</td>
<td>187</td>
<td>275</td>
<td>0.28</td>
<td>493</td>
<td>51.7</td>
<td>64.8</td>
<td>15.35</td>
</tr>
<tr>
<td>Hybrid, $h_{Si} &lt; 200$ nm</td>
<td>188.4</td>
<td>370</td>
<td>0.62</td>
<td>415.7</td>
<td>38.3</td>
<td>62.2</td>
<td>14.7</td>
</tr>
<tr>
<td>ZnO, $h_{Si} &lt; 350$ nm</td>
<td>268</td>
<td>208</td>
<td>0.4</td>
<td>474</td>
<td>57.4</td>
<td>68.2</td>
<td>16.14</td>
</tr>
</tbody>
</table>
rently disagree about the maximum achievable short-circuit current always easy to make accurate comparisons especially when it is likely to happen, otherwise, the absorptions spectra of our structures compare very well but it presents slightly better properties (14.7 mA/cm$^2$). Other than that, the anti-reflective coating only.

These performances can be compared either to similar optimized structures or to cells based on a thin (around 100 nm thick) patterned amorphous silicon layer. It is not always easy to make accurate comparisons especially when we disagree about the maximum achievable short-circuit current $j_0$ (Ref. 6). It still appears that the performances of the structures we have proposed are really good for so thin active layers. For instance, with an optimized cell very similar to ours, Kroll et al. reach 14.4 mA/cm$^2$ (according to our simulations, for the spectral range considered here) with a thick anti-reflective coating and a 338 nm thick silicon layer. According to our results, this performance could have been obtained with a 94 nm thick layer and a very thin ZnO layer instead, but to be fair, we should compare to the composite structure (the thin ZnO layer would not be electrically realistic) that presents a 13.8 mA/cm$^2$ short-circuit current only. The second optimum is based on a 188 nm thick active layer, but it presents slightly better properties (14.7 mA/cm$^2$). Otherwise, the absorption spectra of our structures compare very well with cells in which recombinations are much more likely to happen, reaching similar performances. Finally, Zanotto et al. see a 12.4% increase of $j_{sc}$ due to a patterning of the active layer that we were able to attain by patterning the anti-reflective coating only.

**IV. CONCLUSION**

The thorough physical analysis we have conducted here shows that the resonances occurring in very thin solar cells with a flat active layer of a-Si:H typically thinner than 200 nm and anti-reflective coatings based on a roughly 50 nm thick homogeneous layer of ZnO or ITO) have more impact on the conversion efficiency than for much thicker structures. For these very thin structures, the short-circuit current is, for instance, not a strictly increasing function of the silicon layer. This means that there are pronounced local maxima of the conversion efficiency for flat anti-reflective coatings as well as patterned anti-reflective coatings (increasing the efficiency by at least 10% for our thinnest structures compared to flat coatings). We have used a genetic algorithm guided by our physical analysis to find these locally optimal structures.

This kind of structure, with a flat and very thin active layer, is particularly interesting because (1) the recombinations are minimized, conversely to approaches based on the patterning of the active layer and (2) it represents a very efficient use of the silicon to convert light into electron–hole pairs. We have actually obtained a short-circuit current of 13.8 mA/cm$^2$ for a structure with a 96.5 nm thick only silicon layer (corresponding to a 58.15% conversion efficiency over the 375–750 nm range). This structure has a composite anti-reflective coating made of a 30 nm thick ITO layer with a patterned ZnO layer on top of it, which allows one to combine the optical properties (high index and low losses) of ZnO with the electrical properties of ITO.

Using the same methodology, more complex photonic patterns can be considered, for example, leading to a reduced dependence on the incident light polarization or to an absorption enhancement over a wider wavelength range. This includes two-dimensional patterns or multi-scale structures, for which a simple geometrical parameter scanning is not appropriate to provide a relevant optimization of the design.

**ACKNOWLEDGMENTS**

The authors would like to thank Stéphane Larouche for fruitful discussions and simulations concerning the anti-reflective behavior of the grating and Rémi Polle for the help with Fig. 7.

**APPENDIX**

The absorption inside the active a-Si:H layer is computed using either the scattering matrix method for the flat coating or a Fourier modal method for a patterned electrode. The absorption is obtained by the difference between the flux of the Poynting vector at the upper and the lower interfaces of the silicon layer, when the incident power is normalized to one. In TM polarization, this flux can be written as

$$\Phi_m = \Re \left( \sum_n \frac{1}{2 \varepsilon_0 c \varepsilon_r} \gamma_n (A_n^* B_n^* - A_n^* B_n^* \varepsilon_n + B_n^* A_n^*) \right),$$

where $A_n$ and $B_n$ are the amplitudes of mode $n$ in the silicon layer (propagating or decreasing downward and upward, respectively), $\gamma_n = \sqrt{\varepsilon_n n^2 - (2 \pi n/d)^2}$ its propagation...
constant, $\varepsilon_r$ the permittivity of $\alpha$-Si:H, $k_0$ the wavenumber in vacuum, and $d$ the period of the grating. In TE polarization, the flux can be written as

$$\Phi_E = \omega \left( \sum_n \frac{1}{2\omega k_0} r_n^2 (A_n - B_n)(A_n^* + B_n^*) \right). \quad (A2)$$

For a flat structure, the flux is computed considering only the 0th order ($n = 0$) and there is no need to make any difference between the two polarizations in normal incidence. The conversion efficiency is averaged on TE and TM polarization when the absorption is different for the two polarizations.